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Interpolation Formulas for Viscosity of Six Gases: Air, Nitrogen, Carbon Dioxide, Helium, Argon, and Oxygen

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## Interpolation Formulas for Viscosity of Six Gases: Air, Nitrogen, Carbon Dioxide, Helium, Argon, and Oxygen

Frank E. Jones

Center for Chemical Engineering National Engineering Laboratory National Bureau of Standards Washington, D C 20234



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INTERPOLATION FORMULAS FOR VISCOSITY OF SIX GASES:
AIR, NITROGEN, CARBON DIOXIDE, HELIUM, ARGON, AND OXYGEN

Frank E. Jones
National Bureau of Standards
Washington, DC 20234

Equations for the calculation of viscosity for dry air, nitrogen, carbon dioxide, helium, argon, and oxygen have been developed as interpolation formulas fitted to experimental data. The approximate ranges of strict application of the equations are the ranges of temperature (20°C  $\leq$  t  $\leq$  50°C) and pressure (0.04  $\leq$  p  $\leq$  4 MPa; 0.4  $\leq$  p  $\leq$  40 atm) for the experimental data. The estimates of relative residual standard deviation for the fits (0.05% for air, 0.03% for nitrogen, 0.02% for carbon dioxide, 0.02% for helium, 0.03% for argon, and 0.03% for oxygen) are in close agreement with estimates of precision for the experimental data.

Key words: Air; argon; calculation; carbon dioxide; helium; nitrogen; oxygen; viscosity.

#### 1. INTRODUCTION

In the calibration and use of flow metering devices the precise, accurate value of the viscosity of the gas being metered is often required. The availability of simple equations relating viscosity,  $\mu$ , to temperature, t, and pressure, p, would be a convenience to the engineer in calculating  $\mu$ . In the present work, simple interpolation formulas have been developed which enable the engineer to conveniently make precise, accurate calculations of  $\mu$  for dry air, nitrogen, carbon dioxide, helium, argon, and oxygen using small readily available hand-held calculators. The formulas are fitted to experimental data. The data were selected from the literature on the basis of claimed accuracy and precision, and of internal consistency. The last of these criteria is particularly important for the development of empirical equations for volume flow with a dominant term of the Poiseuille form, the subject of a later paper. The sets of data published by Kestin and

his collaborators [1-10] meet these criteria and have been used to develop the formulas.

#### 2. EXPERIMENTAL DATA

The ranges of temperature and pressure of interest in the present work are  $0^{\circ}$ C < t <  $50^{\circ}$ C and 0 < p < 4 MPa (0 < p < 40 atm). The experimental data used in developing the equations for  $\mu$  are listed in Tables 1-6. In Table'l for dry air, the data in the first and third groups are taken from Table III of [1]; the second and fourth groups are taken from Table II of [2]; and the 50.00°C point is inferred from the data in [2]. In Table 2 for nitrogen, the first and third groups are taken from Table XI of [1]; the second, fifth, and sixth groups are taken from Table VIII of [2]; the fourth group is taken from Table III of [3]; the 20.58°C point is taken from Table XI of [1]; and the 24.920°C point is taken from Table III of [3]. In Table 3 for carbon dioxide, the 20.00°C data are taken from Table V of [1]; the second group is taken from Table IV of [2]; and the 25.00°C point is taken from Table III of [4]. In Table 4 for helium, the first group is taken from Table VII of [1]; the 25.00°C point is taken from Table IV of [5]; and the third group is taken from Table V of [2]. In Table 5 for argon, the first and second groups are taken from Table IV of [1]; the third group is taken from Table IV of [3]; and the fourth group is taken from Table III of [2]. In Table 6 for oxygen, the first and second groups are adjusted values from Table XII of [1]; the third group is taken from Table V of [10].

### 3. DEVELOPMENT OF EQUATIONS

The equations for  $\mu$  (t,p) were developed using a procedure [6] in which  $\mu$ (t,p) is expressed as

$$\mu(t,p) = \mu_0 (t,0) + \Delta \mu(p).$$
 (1)

where  $\mu_0$  (t,0) is the viscosity at "zero pressure" and  $\Delta\mu$ (p) is the experimental value of viscosity,  $\mu_{meas}$ , minus  $\mu_0$  (t,0). The procedure will be outlined below.

### Air

The data pairs, (20.00°C, 181.94  $\mu g/cm \cdot s$ ), (23.44°C, 183.75  $\mu g/cm \cdot s$ ), (23.90°C, 184.21  $\mu g/cm \cdot s$ ), (25.00°C, 184.62  $\mu g/cm \cdot s$ ), and (50.00°C, 197.31  $\mu g/cm \cdot s$ ), taken from Table 1, were fitted by least squares to an equation quadratic in t to enable calculation of  $\mu$  at 0.101325 MPa,  $\mu_1$ . The small departures of p from this value of pressure for these pairs are not significant. The resulting equation is

$$\mu_1 = 170.368 + 0.605434 t - 1.33200 \times 10^{-3} t^2,$$
 (2)

where  $\mu_l$  is in  $\mu g/cm \cdot s$  and t is in °C. To reduce  $\mu_l$  to "zero pressure,"  $\mu_0$ , the value of the increase in  $\mu$  per 0.10325 MPa, 0.11  $\mu g/cm \cdot s$ , estimated from the tabulated data was subtracted from  $\mu_l$  resulting in

$$\mu_0 = 170.258 + 0.605434 t - 1.33200 \times 10^{-3} t^2$$
. (3)

Calculated values of  $\mu_{\Omega}$  are listed in Table 1.

The difference,  $\Delta\mu$ , between the experimental values of  $\mu$  and calculated values of  $\mu_0$  is also listed in Table 1. The values of  $\Delta\mu$  were fitted by least squares to an equation quadratic in p. The resulting equation is

$$\Delta \mu = -2.44358 \times 10^{-3} + 1.17237 p + 0.125541 p^2.$$
 (4)

Equations (3) and (4) were added together to synthesize the final equation for calculating  $\mu$ :

$$\mu_{\text{calc.}} = \mu_{\text{o}} + \Delta \mu = 170.256 + 0.605434 \text{ t} - 1.33200 \text{ x} \cdot 10^{-3} \text{ t}^2$$

$$+ 1.17237 \text{ p} + 0.125639 \text{ p}^2, \tag{5}$$

where  $\mu_{calc.}$  is in  $\mu g/cm \cdot s$ , t is in  $\underline{{}^{\circ}C}$ , and p is in  $\underline{MPa}$ . Values of  $\mu_{calc.}$  and differences between  $\mu_{calc.}$  and experimental values,  $\mu_{meas.}$ , are listed in Table 1.

The estimate of residual standard deviation (RSD), that is, the estimate of the standard deviation of  $\mu_{\text{calc.}}^{-\mu_{\text{meas.}}}$ , is  $0.10~\mu\text{g/cm} \cdot \text{s}$  for the 19 differences (n=19). The estimate of the relative residual standard deviation (RRSD), that is, the ratio of RSD to the mean  $\mu_{\text{meas.}}$ , is 0.05%. Kestin and Leidenfrost [1] estimated that for their measurements "a precision ranging from  $\pm 0.01\%$  to  $\pm 0.07\%$ , depending on the gas, has been achieved. The final accuracy of the measurements is estimated to be of the order of  $\pm 0.05\%$ ." DiPippo and Kestin [2] estimated the precision of their data to be  $\pm 0.05\%$ ; they reached the conclusion that "no meaningful assessment of the accuracy of the present data can be given if by accuracy we mean the irreducible discrepancy between the best measurements available at any particular time."

For  $\mu$  in  $\mu Pa \cdot s$ , t in C, and p in MPa, equation (5) becomes

$$\mu_{\text{calc.}} = 17.0256 + 6.05434 \times 10^{-2} \text{ t} -1.33200 \times 10^{-4} \text{ t}^2$$

$$+ 0.117237 \text{ p} + 1.25639 \times 10^{-2} \text{ p}^2. \tag{6}$$

For  $\mu$  in  $10^{-6}$  1b ft<sup>-1</sup> sec<sup>-1</sup>, t in °C, and p in PSI, equation (5) becomes

$$\mu_{\text{calc.}} = 11.4407 + 4.06833 \times 10^{-2} \text{ t} -8.95063 \times 10^{-5} \text{ t}^2$$
  
+ 5.43165 × 10<sup>-4</sup> p + 4.01338 × 10<sup>-7</sup> p<sup>2</sup>. (7)

## Nitrogen

The data pairs, (20.58°C, 175.93  $\mu$ g/cm·s), (21.98°C, 176.56  $\mu$ g/cm·s), (23.15°C, 177.05  $\mu$ g/cm·s), (24.920°C, 177.94  $\mu$ g/cm·s), (29.75°C, 180.08  $\mu$ g/cm·s), and (49.37°C, 189.71  $\mu$ g/cm·s), taken from Table 2, were fitted by least squares to an equation quadratic in t to enable calculation of  $\mu$ 1. The resulting equation is

$$\mu_1 = 167.335 + 0.392728 t + 1.22474 \times 10^{-3} t^2$$
. (8)

To reduce  $\mu_1$  to  $\mu_0,$  0.11  $\mu g/cm \cdot s$  estimated from the tabulated data was subtracted from  $\mu_1$  resulting in

$$\mu_0 = 167.225 + 0.392728 t + 1.22474 \times 10^{-3} t^2$$
. (9)

The values of  $\Delta\mu$  were fitted by least squares to an equation quadratic in p. The resulting equation is

$$\Delta \mu = -1.12860 \times 10^{-2} + 1.24165 p + 9.87206 \times 10^{-2} p^2$$
. (10)

Equations (9) and (10) were added together to synthesize the final equation for calculating  $\mu$ :

$$\mu_{\text{calc.}} = 167.214 + 0.392728 \text{ t} + 1.22474 \times 10^{-3} \text{ t}^2$$

$$+ 1.24165 \text{ p} + 9.87206 \times 10^{-2} \text{ p}^2, \tag{11}$$

where  $\mu_{calc.}$  is in  $\mu g/cm \cdot s$ , t is in  $\underline{\,}^{\circ}C$ , and p is in  $\underline{MPa}$ .

The RSD is  $0.05~\mu g/cm \cdot s$  for n = 50; the RRSD is 0.03%. Kestin et. al. [3] estimated the accuracy of their experimental measurements to be of the order of  $\pm 0.2\%$  and the relative precision to be 0.03%. The accuracy and precision estimates quoted above for air from [1] and [2] apply also to nitrogen.

For  $\mu$  in  $\mu$ Pa·s, t in °C, and p in MPa, equation (11) becomes

$$\mu_{\text{calc.}} = 16.7214 + 3.92728 \times 10^{-2} \text{ t} + 1.22474 \times 10^{-4} \text{ t}^2$$

$$+ 0.124165 \text{ p} + 9.87206 \times 10^{-3} \text{ p}^2. \tag{12}$$

For  $\mu$  in  $10^{-6}$  1b ft<sup>-1</sup> sec<sup>-1</sup>, t in °C, and p in PSI, equation (11) becomes

$$\mu_{\text{calc.}} = 11.2363 + 2.63901 \times 10^{-2} \text{ t} + 8.22987 \times 10^{-5} \text{ t}^2$$

$$+ 5.75263 \times 10^{-4} \text{ p} + 3.15351 \times 10^{-7} \text{ p}^2. \tag{13}$$

## Carbon Dioxide

The data pairs, (20.00°C, 146.63  $\mu$ g/cm·s), (25.00°C, 149.09  $\mu$ g/cm·s), (30.40°C, 151.81  $\mu$ g/cm·s), and (49.12°C, 161.75  $\mu$ g/cm·s), taken from Table 3, were fitted by least squares to an equation quadratic in t to enable calculation of  $\mu$ <sub>1</sub>. The resulting equation is

$$\mu_1 = 137.335 + 0.441133 t + 1.12987 \times 10^{-3} t^2$$
. (14)

To reduce  $\mu_1$  to  $\mu_0$ , 0.13  $\mu g/cm \cdot s$  estimated from the tabulated data was subtracted from  $\mu_1$  resulting in

$$\mu_0 = 137.205 + 0.441133 t + 1.12987 x 10^{-3} t^2$$
. (15)

The values of  $\Delta_\mu$  were fitted by least squares to an equation quadratic in p. The resulting equation is

$$\Delta_{\text{u}} = 0.133827 + 6.28105 \times 10^{-2} \text{ p} + 0.562974 \text{ p}^2.$$
 (16)

Equations (15) and (16) were added together to synthesize the final equation for calculating  $\mu$ :

$$\mu_{\text{calc.}} = 137.339 + 0.441133 t + 1.12987 \times 10^{-3} t^2 + 6.28105 \times 10^{-2} p + 0.562974 p^2,$$
 (17)

where  $\mu_{calc.}$  is in  $\mu g/cm \cdot s$ , t is in C, and p is in MPa.

The RSD is  $0.04 \, \mu g/cm \cdot s$  for n = 11; the RRSD is 0.02%. Kestin et. al. [4] estimated the accuracy of the 25.00°C point, "expressed as the maximum

estimated uncertainty in the quoted values," to be  $\pm 0.1\%$ . The accuracy and precision estimates quoted above for air from [1] and [2] apply also to carbon dioxide.

For  $\mu$  in  $\mu Pa \cdot s$ , t in C, and p in MPa, equation (17) becomes

$$\mu_{\text{calc.}} = 13.7339 + 4.41133 \times 10^{-2} \text{ t} + 1.12987 \times 10^{-4} \text{ t}^2$$

$$+ 6.28105 \times 10^{-3} \text{ p} + 5.62974 \times 10^{-2} \text{ p}^2. \tag{18}$$

For  $\mu$  in  $10^{-6}$  1b ft<sup>-1</sup> sec<sup>-1</sup>, t in  $^{\circ}$ C, and p in  $^{\circ}$ PSI, equation (17) becomes

$$\mu_{\text{calc.}} = 9.22876 + 2.96428 \times 10^{-2} \text{ t} + 7.59238 \times 10^{-5} \text{ t}^2$$

$$+ 2.91005 \times 10^{-5} \text{ p} + 1.79836 \times 10^{-6} \text{ p}^2. \tag{19}$$

## Helium

The data pairs, (20.00°C, 196.14  $\mu g/cm \cdot s$ ), (24.28°C, 198.19  $\mu g/cm \cdot s$ ), (25.00°C, 198.59  $\mu g/cm \cdot s$ ), (30.56°C, 201.18  $\mu g/cm \cdot s$ ), and (52.79°C, 211.04  $\mu g/cm \cdot s$ ), were fitted by least squares to an equation quadratic in t to enable calculation of  $\mu_1$ . The effect of pressure on  $\mu$  for helium is so small that no correction is made to reduce  $\mu_1$  to  $\mu_0$ . The resulting equation is

$$\mu_1 = \mu_0 = 185.946 + 0.530773 t - 1.04982 x  $10^{-3} t^2$ . (20)$$

The values of  $\Delta\mu$  were fitted by least squares to an equation linear in p. The resulting equation is

$$\Delta u = 2.91664 \times 10^{-2} - 6.99813 \times 10^{-2} p.$$
 (21)

Equations (20) and (21) were added together to synthesize the final equation for calculating  $\mu$ :

$$\mu_{\text{calc.}} = 185.975 + 0.530773 \text{ t} - 1.04982 \times 10^{-3} \text{ t}^2$$

$$- 6.99813 \times 10^{-2} \text{ p}, \qquad (22)$$

where  $\mu_{calc}$  is in  $\mu g/cm \cdot s$ , t is in C, and p is in MPa.

The RSD is 0.04  $\mu$ g/cm·s for n = 15; the RRSD is 0.02%. The accuracy and precision estimates quoted above for air from [1] and [2] apply also to helium. The 25.00°C °C value is estimated to be accurate within  $\pm$  0.1% [5].

For  $\mu$  in  $\mu$ Pa·s, t in °C, and p in MPa, equation (22) becomes

$$\mu_{\text{calc.}} = 18.5975 + 5.30773 \times 10^{-2} \text{ t} - 1.04982 \times 10^{-4} \text{ t}^2$$

$$- 6.99813 \times 10^{-3} \text{ p.} \tag{23}$$

For  $\mu$  in  $10^{-6}$  1b ft<sup>-1</sup> sec<sup>-1</sup>, t in  $\underline{^{\circ}C}$ , and p in  $\underline{PSI}$ , equation (22) becomes

$$\mu_{\text{calc.}} = 12.4969 + 3.56663 \times 10^{-2} \text{ t} - 7.05446 \times 10^{-5} \text{ t}^2$$

$$- 3.24228 \times 10^{-5} \text{ p.}$$
(24)

## Argon

The data pairs, (20.00°C, 222.86  $\mu$ g/cm·s), (24.39°C, 225.79  $\mu$ g/cm·s), (25.00°C, 226.36  $\mu$ g/cm·s), and (50.31°C, 243.43  $\mu$ g/cm·s), taken from Table 5, were fitted by least squares to an equation quadratic in t to enable calculation of  $\mu$ <sub>1</sub>. The resulting equation is

$$\mu_1 = 208.940 \div 0.702190 t - 3.30712 \times 10^{-4} t^2$$
. (25)

To reduce  $\mu_1$  to  $\mu_0,~0.21~\mu g/cm\cdot s$  estimated from the tabulated data was subtracted from  $\mu_1$  resulting in

$$\mu_0 = 208.730 + 0.702190 t - 3.30712 \times 10^{-4} t^2$$
. (26)

The values of  $\Delta \mu$  were fitted by least squares to an equation quadratic in p. The resulting equation is

$$\Delta \mu = 3.17420 \times 10^{-2} + 1.73987 p + 0.152358 p^2$$
. (27)

Equations (26) and (27) were added together to synthesize the final equation for calculating  $\mu$ :

$$\mu_{\text{calc.}} = 208.762 + 0.702190 \text{ t} - 3.30712 \times 10^{-4} \text{ t}^2$$
 $+ 1.73987 \text{ p} + 0.152358 \text{ p}^2,$  (28)

where  $\mu_{calc.}$  is in  $\underline{\mu g/cm \cdot s}$ , t is in  $\underline{{}^{\circ}C}$ , and p is in  $\underline{MPa}$ .

The RSD is 0.07  $\mu$ g/cm·s for n = 38; the RRSD is 0.03%. The estimates of accuracy and precision of the experimental data for argon are those quoted above from [1], [2], and [3].

For  $\mu$  in  $\underline{\nu}$ Pa·s, t in  $\underline{\circ}$ C, and p in  $\underline{MPa}$ , equation (28) becomes

$$\mu_{\text{calc.}} = 20.8762 + 7.02190 \times 10^{-2} \text{ t} - 3.30712 \times 10^{-5} \text{ t}^2$$
  
+ 0.173987 p + 1.52358 x  $10^{-2}$  p<sup>2</sup>.

(29)

$$\mu_{\text{calc.}} = 14.0282 + 4.71850 \times 10^{-2} \text{ t} - 2.22228 \times 10^{-5} \text{ t}^2 + 8.06091 \times 10^{-4} \text{ p} + 4.86689 \times 10^{-7} \text{ p}^2.$$
 (30)

#### 0xygen

The data pairs, (20.00°C, 203.17  $\mu$ g/cm·s), (25.00°C, 206.25  $\mu$ g/cm·s), (35.00°C, 212.18  $\mu$ g/cm·s), and (50.00°C, 220.80  $\mu$ g/cm·s), taken from Table 6, were fitted by least squares to an equation quadratic in t to enable calculation of  $\mu$ 1. The resulting equation is

$$\mu_1 = 190.539 + 0.650043 t - 8.97542 \times 10^{-4} t^2$$
. (31)

To reduce  $\mu_1$  to  $\mu_0$ , 0.12  $\mu g/cm \cdot s$  estimated from the tabulated data was subtracted from  $\mu_1$  resulting in

$$\mu_0 = 190.419 + 0.650043 t - 8.97542 \times 10^{-4} t^2$$
. (32)

The values of  $\Delta \mu$  were fitted by least squares to an equation quadratic in p. The resulting equation is

$$\Delta \mu = -0.0239595 + 0.130897 p + 1.323418 x 10^{-3} p^2$$
. (33)

Equations (32) and (33) were added together to synthesize the final equation for calculating  $\mu$ :

$$\mu_{\text{calc.}} = 190.395 + 0.650043 \text{ t} - 8.97542 \times 10^{-4} \text{ t}^2 + 0.130897 \text{ p} + 1.32418 \times 10^{-3} \text{ p}^2$$
 (34)

where  $\mu_{calc}$  is in  $\mu g/cm \cdot s$ , t is in °C, and p is in atm.

The RSD is  $0.06\,$  g/cm s for n = 16; the RRSD is 0.03%. The estimates of accuracy and precision of the experimental data for oxygen are those quoted above from [1], [2], and [3].

For  $\mu$  in  $\mu Pa \cdot s$ , t in C, and p in MPa, equation (34) becomes

$$\mu_{\text{calc.}} = 19.0395 + 6.50043 \times 10^{-2} \text{ t} - 8.97542 \times 10^{-5} \text{ t}^2 + 0.129185 \text{ p} + 1.28975 \times 10^{-2} \text{ p}^2.$$
 (35)

For  $\mu$  in  $10^{-6}$  1b ft<sup>-1</sup> sec<sup>-1</sup>, t in °C, and p in PSI, equation (34) becomes

calc. = 
$$12.7940 + 4.36809 \times 10^{-2} t - 6.03121 \times 10^{-5} t^{2}$$
  
+  $5.98525 \times 10^{-4} p + 4.11587 \times 10^{-7} p^{2}$ . (36)

## 4. RANGES OF APPLICATION OF THE EQUATIONS

The equations developed in this paper are <u>interpolation</u> formulas fitted to experimental data. The range of strict application is indicated by the range of t and p of the experimental data listed in Tables 1-5. In the absence of measurements of  $\mu$  for temperatures below 20°C of comparable quality to that of the data in the tables, there are two options in extending calculations <u>below</u> 20°C (0 < t < 20°C): 1) apply the extended law of corresponding states [3,7-10]; 2) <u>extrapolate</u> using the equations developed here, with probable loss in accuracy. Either option might be followed until suitable experimental data at temperatures below 20°C became available.

Hanley et al. [11] have developed a functional form to represent critically evaluated viscosity and thermal conductivity coefficient data, and have generated tables. The gases treated by Hanley et al. include nitrogen and argon. Values of  $\mu$  calculated using the formulas in the present work have been compared with interpolated values from the tables in [11] at 0°C, 5°C, 10°C, 15°C, 20°C, and 25°C, and 0.1 MPa, for nitrogen and argon. The deviation of the values in the present work from the values from reference [11], expressed in percent are: for nitrogen, +0.26% at 0°C, +0.02% at 5°C, -0.12% at 10°C, -0.28% at 15°C, -0.32% at 20°C, and -0.38% at 25°C; for argon, -1.16% at 0°C, -1.10% at 5°C, -0.99% at 10°C, -0.86% at 15°C, -0.78% at 20°C, and -0.66% at 25°C. These deviations are all well within the uncertainty, + 2%, estimated by Hanley et al. for their tables.

#### 5. CONCLUSIONS

Equations (interpolation formulas fitted to experimental data) for the calculation of  $\mu$  for dry air, nitrogen, carbon dioxide, helium, argon, and oxygen have been developed. The estimates of relative residual standard deviation for the fits are in close agreement with the estimates of precision for the experimental data in the above stated ranges.

#### 6. ACKNOWLEDGMENTS

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## Nomenclature

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p = pressure 

RRSD = estimate of relative residual standard deviation 

RSD = estimate of residual standard deviation 

t = temperature in °C 

\Delta \mu = \mu_{meas}.^{-\mu}o
\mu = viscosity
\mu_{calc}. = calculated value of viscosity
\mu_{meas}. = experimental value of viscosity
\mu_{o} = viscosity at "zero pressure"
\mu_{1} = viscosity at 0.101325 MPa
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Table 1

		<sup>μ</sup> calcμmeas. (μg/cm⋅s)	+0.01 -0.01 0.00 0.00	-0.01	+0.10 +0.02 -0.11 -0.12 -0.07	+0.06 +0.14 +0.14	+0.05
		$^{\mu}$ calc. $_{(\mu g/cm.s)}$	181.95 182.37 182.83 183.32	184.39 184.96 187.56	183.85 184.47 184.22 184.09 184.06	184.68 187.12 190.32	197.36 197.04
	4ir	$^{\Delta\mu}_{\mu g/cm \cdot s}$ )	0.11 0.55 1.01 2.05	2.67 3.15 5.87	0.03 0.06 0.31 0.24 0.17 0.08	0.06 2.42 5.62	0.08
- - - -	Viscosity of Dry Air	η (πg/cm·s)	181.83 181.83 181.83	181.83 181.83	183.72 184.39 184.02 183.97 183.96	184.56 184.56 184.56	197.16 196.91
		μmeas. (μg/cm⋅s)	181.94 182.38 182.84 183.32	184.40 184.98 187.70	183.75 184.45 184.33 184.21 184.13	184.62 186.98 190.18	197.25 196.99 197.31
		Press., P, (atm)	1.00 4.39 7.79 11.22	18.03 21.40 34.97	1.07 0.69 1.71 1.04 0.83	1.00 18.01 35.12	1.70
		Temp., t, (C)	20.00 20.00 20.00	20.00	23.44 24.68 24.00 23.90 23.89 23.97	25.00 24.99 24.99	49.91 49.39 <sup>a</sup> 50.00

aUsed for calculating µ1 only.

Table 2

"calc.-"meas. (s•mo/gn) -0.07 -0.08 +0.02 +0.13 +0.10 +0.07 0.00 +0.03 +0.02 +0.03 -0.03 +0.04 +0.04 +0.03 +0.03 +0.05 +0.04 -0.04 +0.01 -0.04 μg/cm·s) ucalc. 181.17 178.56 178.16 177.61 176.60 176.13 175.69 175.65 176.54 176.57 177.77 177.85 177.90 177.99 178.02 178.02 184.84 182.16 179.85 178.84 (s·w)/gm) 5.67 3.07 2.57 2.01 1.39 0.93 0.12 0.05 0.17 0.25 0.25 0.18 0.18 0.16 0.16 0.11 6.98 4.31 2.08 1.02 0.15 Viscosity of Nitrogen (s·mo/gn) 176.35 176.45 177.55 177.61 177.68 177.84 177.88 177.88 175.57 175.57 175.57 175.57 175.57 175.57 175.57 175.57 177.81 177.81 177.81 177.81 μg/cm⋅s) 181.24 178.64 178.14 177.58 176.96 176.06 175.69 175.62 176.52 176.56 177.84 177.86 177.86 177.99 177.99 184.79 182.12 179.89 178.83 Press., P, (atm) 34.82 20.48 18.04 14.59 11.17 7.79 4.38 1.00 0.687 0.385 41.86 28.21 14.60 7.80 0.991 Temp., t, (C) 20.00 20.00 20.00 20.00 20.00 20.00 20.00 21.75 21.98 24.44 24.72 24.84 25.07 25.15 23.22 23.22 25.00 25.00 25.00 25.00 25.00

Table 2 (continued)

	$^{\mu}$ calc $^{\mu}$ meas. $^{(\mu g/cm.s)}$	-0.05 -0.04 -0.04 -0.05 -0.05 -0.05 -0.05 -0.05 -0.03 -0.03 -0.03 -0.03 -0.03 -0.03 -0.03 -0.03
	μcalc. (μg/cm·s)	178.02 178.02 178.02 178.19 178.28 178.45 178.45 178.68 178.77 178.68 179.90 180.73 181.52 182.46 183.41 180.20 189.98 189.98
	Δμ (μg/cm·s)	0.07 0.32 0.33 0.032 0.053 1.00 1.00 0.053 3.64 6.62 0.09 0.09 0.09
Nitrogen	μο (μg/cm·s)	177.81 177.81 177.81 177.81 177.81 177.81 177.81 177.81 177.81 177.81 177.81 177.81 177.81 177.81 177.81 189.99 189.08
	μmeas. (μg/cm·s)	177.98 178.06 178.06 178.13 178.32 178.41 178.41 178.90 179.04 179.04 179.04 179.04 179.04 179.04 179.04 179.04 179.04 179.04 179.04 179.04 189.45 181.45 182.49 189.08 180.01 189.98 189.01 189.98
	Press., P, (atm)	1.000 1.714 2.300 3.009 3.715 4.341 4.979 6.613 7.307 8.954 9.931 14.830 20.051 24.644 29.838 34.816 39.919 1.06 1.06
	Temp., t, (C)	25.00 25.00

<sup>a</sup>Used for calculating μ<sub>1</sub> only.

Table 3

	<sup>μ</sup> calc <sup>μ</sup> meas. (μg/cm·s)	-0.01	+0.02	00.00	-0.03	0.00	+0.06	-0.04	0.00	00.0	00.00
	μcalc. (μg/cm·s)	148.61	147.41	147.01	146.75	146.63	146.62	151.79	151.81	161.75	149.09
∽bon Dioxide	Δ <sub>μ</sub> (μg/cm·s)	2.14	0.91	0.53	0.30	0.15	0.08	0.20	0.15	0.15	0.15
Viscosity of Carbon Dioxide	μ <sub>O</sub> (μg/cm·s)	146.48 146.48	146.48	146.48	146.48	146.48	146.48	151.63	151.66	161.60	148.94
	μmeas. (μg/cm·s)	148.62	147.39	147.01	146.78	146.63	146.56	151.83	151.81	161.75	149.09
	Press., P, (atm)	18.02	11.13	7.78	4.38	0.976	0.640	1.69	1.06	1.08	1.00
	Temp., t, (C)	20.00	20.00	20.00	20.00	20.00	20.00	30.34	30.40	49.12	25.00

Table 4

<b>a</b>	Viscosity of Helium	tas. $^{\mu}o$ $^{\lambda}\mu$ $^{\mu}calc^{\mu}meas.$ $^{\mu}cm.s)$ $^{\mu}cm.s)$ $^{\mu}cm.s)$ $^{\mu}calc^{\mu}meas.$	5.94 196.14 -0.20 195.92 -0.02 5.99 196.14 -0.15 196.02 +0.03 5.02 196.14 -0.12 196.04 +0.02	196.14	196.14 +0.05 196.14 196.14 0.00 196.16	198.56 +0.03 198.58 -0.01	3.12       198.08       +0.04       198.10       -0.02         3.19       198.21       -0.02       198.23       +0.04         .20       201.15       +0.05       201.17       -0.03         .18       201.19       -0.01       201.21       +0.03         .16       211.13       +0.03       211.15       -0.01
<b>a</b>	Viscosity of Helium	ηον (πg/cm·s)					
0 > 0 <		oress., P, umeas. (atm) (ug/cm·s)					1.57 198.12 1.06 198.19 1.71 201.20 1.07 201.18 1.61 211.16

Table 5

	<sup>μ</sup> calc <sup>μ</sup> meas. (μg/cm·s)	-0.07 -0.04 -0.01 -0.03 -0.01	+0.02 +0.18 +0.06 +0.01	+0.05 +0.03 +0.00 +0.00 +0.00 +0.00 +0.00 +0.00 +0.00
	$^{\mu}$ calc. $_{\mu g/cm \cdot s})$	229.59 227.17 226.37 225.59 224.85 223.47 222.85 222.86	232.23 230.60 229.02 227.58 226.29	226.29 226.48 226.66 226.66 227.05 227.23 227.74 228.04 228.54 230.33 231.38 234.24 235.72
Argon	Δμ (μg/cm·s)	+7.02 +4.52 +3.77 +2.94 +1.54 +0.09	+6.13 +4.34 +2.88 +1.49 +0.30	+0.26 +0.37 +0.62 +1.05 +1.17 +1.17 +2.04 +4.25 +4.25 +6.75 +86 +86.75
Viscosity of Argon	ο <sub>μ</sub> (s•w)	222.64 222.64 222.64 222.64 222.64 222.64 222.64	226.08 226.08 226.08 226.08	226.08 226.08 226.08 226.08 226.08 226.08 226.08 226.08 226.08 226.08
	μmeas. (μg/cm·s)	229.66 227.16 226.41 225.58 224.86 223.50 222.86 222.73	232.21 230.42 228.96 227.57 226.38	226.34 226.45 226.70 226.70 227.25 227.25 228.12 228.13 230.33 231.36 234.26 235.71
	Press., P, (atm)	30.81 21.42 18.06 14.63 11.22 7.79 4.37 1.00 0.709 0.384	27.91 21.41 14.61 7.81	1.000 2.041 3.034 4.048 5.110 6.035 7.158 8.586 10.029 15.288 20.266 22.637 24.542 29.985 35.156
	Temp., t, (C)	20.00 20.00 20.00 20.00 20.00 20.00	25.00 25.00 25.00 25.00 25.00	25.00 25.00 25.00 25.00 25.00 25.00 25.00 25.00 25.00 25.00

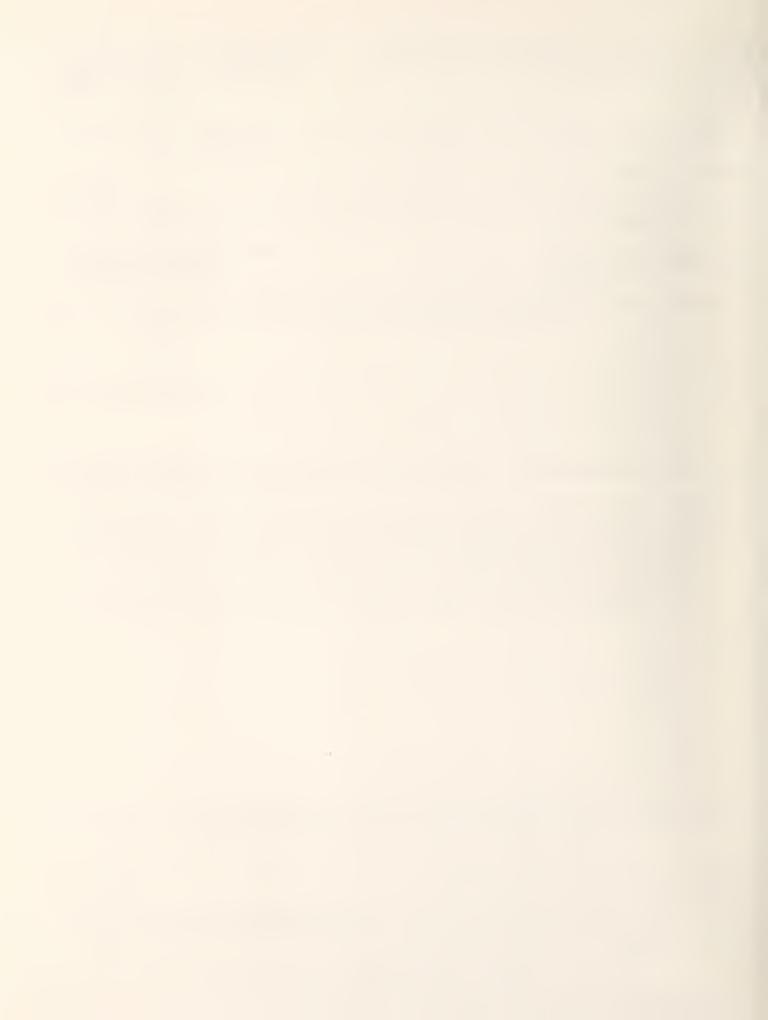
Table 5 (continued)

	<sup>μ</sup> calc <sup>μ</sup> meas. (μg/cm·s)	+0.10 +0.09 -0.25 -0.13 -0.02
	μcalc. (μg/cm·s)	225.93 225.88 242.93 242.92 243.15
	Δμ (μg/cm·s)	+0.21 +0.13 +0.09 +0.42 +0.27
Argon	μ <sub>O</sub> μ(μg/cm·s)	225.62 225.66 242.59 242.63 242.90 243.22
	μmeas. (μg/cm·s)	225.83 225.79 242.68 243.05 243.17
	ress., P, (atm)	1.56 1.07 1.73 1.46 1.22
	Temp., t, Pr (C)	24.33 24.39 49.37 49.43 50.31

	<sup>μ</sup> calc <sup>μ</sup> meas. (μg/cm.s)	-0.13	+0.04 -0.03	+0.01 +0.03	0-0.01	+0.01	+0.03	-0.03	-0.03	-0.01
	μcalc. (μg/cm·s)	206.44	205.23	204.13 203.64	203.17 203.12	213.88	208.28	206.22	206.22	220.79
6 Oxygen	Δμ (μg/cm·s)	3.51	1.64	1.06 0.55	0.07	7.76	2.14	0.14	0.14	0.12
Table 6 Viscosity of Oxygen	μ <sub>ο</sub> (μg/cm·s)	203.06	203.06	203.06	203.06 203.06	206.11	206.11	206.11	206.11	220.68
	μmeas. (μg/cm·s)	206.57	205.19 204.70	204.12 203.61	203.17 203.13	213.87	208.25	206.25	206.25	220.80
	Press., P, (atm)	21.40	11.19	4.39	0.981 0.634	41.83	14.61	0.998		_
	Temp., t, (C)	20.00	20.00 20.00	20.00	20.00	25.00 25.00	25.00	25.00	25.00	50.00

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